

(4)

(b) Define Hasse Diagram & write procedure to construct a Hasse Diagram. 7½

Construct a Hasse Diagram for the partial ordering $\{(A,B) | A \subseteq B\}$ on the power set $P(S)$ where $S = \{a, b, c\}$.

7. (a) Define Lattice. Also describe its properties. 7½

(b) Prove that product of two Lattices is a Lattice. 7½

Unit-IV

8. (a) If $u = \sin^{-1} \frac{x^2 + y^2}{x + y}$, then show that

$$x \frac{\partial u}{\partial x} \cdot y \frac{\partial u}{\partial y} = \tan u \quad 7\frac{1}{2}$$

(b) If $u = \log(x^3 + y^3 + z^3 - 3xyz)$ then show that 7½

$$\left(\frac{\partial}{\partial x} + \frac{\partial}{\partial y} + \frac{\partial}{\partial z} \right)^2 u = \frac{-9}{(x + y + z)^2}$$

9. (a) State & Prove Euler's Theorem. 7½

(b) Solve the following using Chain Rule. 7½

(i) $y = (4x - x^{-5})^{1/2}$

(ii) $y = 2^{\cot x}$

A

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Roll No. _____

SFS-4702

B.C.A. (Semester-II) Examination,

May 2015

Mathematics-II

Paper-V

(BCA-S-110)

Time Allowed : Three Hours] [Maximum Marks :100

Note : Answer five questions in all. Question No. 1 is compulsory and attempt one question from each of the four Units I, II, III & IV.

1. Answer the following : 4 × 10 = 40

(a) Define Finite set, Infinite Set, Singleton set and Universal set with Examples.

(b) If $A = \{1, 2, 3, 4, 5, 6\}$, $B = \{3, 6, 8, 12, 17, 18\}$, then find

(i) $A - B$

(ii) $B - A$

(c) What do you understand by Reflexive relation & Irreflexive relation? Illustrate with an example.

(2)

- (d) Define Function. Differentiate between onto Function & Into function.
- (e) Define Domain & Range of Relation. Give example.
- (f) If $X = \{1, 2, 3, 4, 5, 6\}$, then $/$ is a partial order relation on X . Draw the Hasse Diagram of (X, χ) .
- (g) If $u = x^2y + y^2z + z^2x$, then show that $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = (x + y + z)^2$
- (h) Discuss change of variable?
- (i) Define Duality
- (j) Differentiate $y = \sqrt{13x^2 - 5x + 8}$ by chain Rule.

Unit-I

2. (a) Define sets. Also discuss it's types & algebraic laws of operations of sets. $7\frac{1}{2}$
- (b) (i) Show that $(A \cap B)' = A' \cup B'$
- (ii) $A \cup B = B \cup A$ where A, B are any set. $7\frac{1}{2}$
3. (a) Define ordered pairs and Cartesian Product. Also discuss the properties of Cartesian Product. $7\frac{1}{2}$

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(3)

- (b) (i) Prove that $A \times (B \cap C) = (A \times B) \cap (A \times C)$ $7\frac{1}{2}$
- (ii) If $A = \{4, 5, 7, 8, 10\}$, $B = \{4, 5, 9\}$ and $C = \{1, 4, 6, 9\}$ then verify that $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$

Unit-II

4. (a) Define Partial Order Relation. Is the greater or equal (\geq) relation on the set of integers Z is a Partial Order Relation? Prove it. $7\frac{1}{2}$
- (b) If R be a relation in the set of Integers Z defined by $R = \{(x, y) : x \in Z, y \in Z, (x - y) \text{ is divisible by } 6\}$, then show that R is an equivalence Relation. $7\frac{1}{2}$
5. (a) (i) Discuss functions & it's types. $7\frac{1}{2}$
- (ii) Show that the function $f(x) = x^3$ and $g(x) = x^{1/3}$ for all $x \in R$ are inverse of one another.
- (b) Show that if $f: A \rightarrow B$ & $g: B \rightarrow C$ be one to one onto function, then $g \circ f$ is also one to one onto and $(g \circ f)^{-1} = f^{-1} \circ g^{-1}$. $7\frac{1}{2}$

Unit-III

6. (a) (i) Define Poset & chain.
- (ii) Show that the set Z^+ for all positive integers under divisibility relation forms a poset. $7\frac{1}{2}$

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