### **Time Preference for Money**

**Time preference for money** is an individual's preference for possession of a given amount of money *now*, rather than the same amount at some future time.

Three reasons may be attributed to the individual's time preference for money:

preference for consumption investment opportunities

risk

### **Required Rate of Return**

- The time preference for money is generally expressed by an interest rate. This rate will be positive even in the absence of any risk. It may be therefore called the **risk-free rate**.
- An investor requires compensation for assuming risk, which is called **risk premium**.
- The investor's **required rate of return** is: **Risk-free rate + Risk premium**.

## **Required Rate of Return**

- Would an investor want Rs. 100 today or after one year?
- Cash flows occurring in different time periods are not comparable.
- It is necessary to adjust cash flows for their differences in timing and risk.
- Example : If preference rate =10 percent
  - An investor can invest if Rs. 100 if he is offered Rs 110 after one year.
  - Rs 110 is the future value of Rs 100 today at 10% interest rate.
  - Also, Rs 100 today is the present value of Rs 110 after a year at 10% interest rate.
  - If the investor gets less than Rs. 110 then he will not invest.
     Anything above Rs. 110 is favourable.

## **Time Value Adjustment**

- Two most common methods of adjusting cash flows for time value of money:
  - Compounding—the process of calculating future values of cash flows and
  - Discounting—the process of calculating present values of cash flows.

### **Future Value**

- **Compounding** is the process of finding the future values of cash flows by applying the concept of compound interest.
- **Compound interest** is the interest that is received on the original amount (principal) as well as on any interest earned but not withdrawn during earlier periods.
- **Simple interest** is the interest that is calculated only on the original amount (principal), and thus, no compounding of interest takes place.

#### **Future Value**

 $\textcircled$  The general form of equation for calculating the future value of a lump sum after *n* periods may, therefore, be written as follows:

$$F_n = P\left(1+i\right)^n$$

The term  $(1 + i)^n$  is the **compound value factor** (*CVF*) of a lump sum of Re 1, and it always has a value greater than 1 for positive *i*, indicating that *CVF* increases as *i* and *n* increase.

$$F_n = P \times \text{CVF}_{n,i}$$

### Future Value: Example

✤If you deposited Rs 55,650 in a bank, which was paying a 15 per cent rate of interest on a ten-year time deposit, how much would the deposit grow at the end of ten years?

✤First find out the compound value factor at 15 per cent for 10 years which is 4.046.

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 $FV = 55,650 \times CVF_{10,0.12} = 55,650 \times 4.046 = Rs 225,159.90$ 

### **Future Value of an Annuity**

**Annuity** is a fixed payment (or receipt) each year for a *specified* number of years.

$$F_n = A \left[ \frac{\left(1+i\right)^n - 1}{i} \right]$$

✤ The term within brackets is the compound value factor for an annuity of Re 1, which we shall refer as CVFA.

$$F_n = A \times CVFA_{n,i}$$

# Future Value of an Annuity: Example

Suppose that a firm deposits Rs 5,000 at the end of each year for four years at 6 per cent rate of interest. How much would this annuity accumulate at the end of the fourth year?

€ First find *CVFA* which is 4.3746.

Substituting Sector Activity Sector Sect

 $F_4 = 5,000(\text{CVFA}_{4,0.06}) = 5,000 \times 4.3746 = \text{Rs} \ 21,873$ 

# **Sinking Fund**

- Sinking fund is a fund, which is created out of fixed payments each period to accumulate to a future sum after a specified period. For example, companies generally create sinking funds to retire bonds (debentures) on maturity.
- ✤ The factor used to calculate the annuity for a given future sum is called the *sinking fund factor* (SFF).

$$A = F_n \left[ \frac{i}{\left(1+i\right)^n - 1} \right]$$

#### Example

 Suppose a 20-year-old student wants to start saving for retirement. She plans to save Rs.3 a day. Every day, she puts Rs.3 in her drawer. At the end of the year, she invests the accumulated savings (Rs.1,095) in an online stock account. The stock account has an expected annual return of 12%.

→ When she is 65 years old, she will get Rs. 1,487,261.89

$$A = F_n \left[ \frac{i}{\left(1+i\right)^n - 1} \right]$$

### **Present Value**

- **Present value** of a future cash flow (inflow or outflow) is the amount of current cash that is of equivalent value to the decision-maker.
- **Discounting** is the process of determining present value of a series of future cash flows.
- The *interest rate* used for discounting cash flows is also called the *discount rate*.

### Present Value of a Single Cash Flow

Ge Formula to calculate the present value of a lump sum to be received after some future periods:

$$P = \frac{F_n}{(1+i)^n} = F_n [(1+i)^{-n}]$$

The term in parentheses is the discount factor or present value factor (*PVF*), and it is always less than 1.0 for positive *i*, indicating that a future amount has a smaller present value.

$$PV = F_n \times PVF_{n,i}$$

𝔄 In MS Excel use pv function

**PV**(rate,nper,pmt,fv,type)

#### Example

Suppose that an investor wants to find out the present value of Rs 50,000 to be received after 15 years. Her interest rate is 9 per cent. First, we will find out the present value factor, which is 0.275. Multiplying 0.275 by Rs 50,000, we obtain Rs 13,750 as the present value:

 $PV = 50,000 \times PVF_{15,0.09} = 50,000 \times 0.275 = Rs \ 13,750$ 

## Present Value of an Annuity

The computation of the present value of an annuity can be written in the following general form:

$$P = A\left[\frac{1}{i} - \frac{1}{i\left(1+i\right)^n}\right]$$

✤ The term within parentheses is the present value factor of an annuity of Re 1, which we would call PVFA, and it is a sum of single-payment present value factors.

$$P = A \times \mathbf{PVAF}_{n,i}$$

𝔄 In MS Excel use pmt function.

PMT(rate,nper,pv,fv,type)

### Example

Suppose you have borrowed a 3-year loan of Rs 10,000 at 9 per cent from your employer to buy a motorcycle. If your employer requires three equal end-of-year repayments, then the annual instalment will be

> $10,000 = A \times PVFA_{3,0.09}$  $10,000 = A \times 2.531$  $A = \frac{10,000}{2.531} = Rs 3,951$

## Capital Recovery and Loan Amortisation

Capital recovery is the annuity of an investment made today for a specified period of time at a given rate of interest. Capital recovery factor helps in the preparation of a loan amortisation (loan repayment) schedule.

$$A = P \left[ \frac{1}{\text{PVAF}_{n,i}} \right]$$

 $A = P \times \operatorname{CRF}_{n,i}$ 

She reciprocal of the present value annuity factor is called the *capital recovery factor* (*CRF*).

### Loan Amortisation Schedule

End	Payment	Interest	Principal	Outstanding	
of Year			Repayment	Balance	
0				10,000	
1	3,951	900	3,051	6,949	
2	3,951	625	3,326	3,623	
3	3,951	326	3,625*	0	

# Present Value of an Uneven Periodic Sum

- In most instances the firm receives a stream of uneven cash flows. Thus the present value factors for an annuity cannot be used.
- The procedure is to calculate the present value of each cash flow and aggregate all present values.

### **PV of Uneven Cash Flows: Example**

✤ Consider that an investor has an opportunity of receiving Rs 1,000,Rs 1,500, Rs 800, Rs 1,100 and Rs 400 respectively at the end of one through five years. Find out the present value of this stream of uneven cash flows. The investor's required interest rate is 8 per cent? The present value is calculated as follows:

Present value 
$$= \frac{1000}{(1.08)} + \frac{1,500}{(1.08)^2} + \frac{800}{(1.08)^3} + \frac{1,100}{(1.08)^4} + \frac{400}{(1.08)^5} = Rs3,927.60$$

$$PV = 1,000 \times PVF_{1,.08} + 1,500 \times PVF_{2,.08} + 800 \times$$

$$= PVF_{3,.08} + 1,100 \times PVF_{4,.08} + 400 \times PVF_{5,.08}$$

$$= 1,000 \times .926 + 1,500 \times .857 + 800 \times .794 + 1,100$$

$$\times .735 + 400 \times .681 = Rs3,927.60$$

# **Present Value of Perpetuity**

Perpetuity is an annuity that occurs *indefinitely*. Perpetuities are not very common in financial decision-making.

⇐ The PV of an annuity is:

Present value of a perpetuity =

Perpetuity Interest rate

# **Present Value of a Perpetuity: Example**

⇐Let us assume that an investor expects a perpetual sum of Rs 500 annually from his investment. What is the present value of this perpetuity if his interest rate is 10 per cent?

$$P = \frac{500}{0.10} = \text{Rs} 5,000$$

# Multi-Period Compounding

✤If compounding is done more than once a year, the actual annualised rate of interest would be higher than the nominal interest rate and it is called the effective interest rate.

$$\mathbf{EIR} = \left[1 + \frac{i}{m}\right]^{n \times m} - 1$$